

GEOMETRIC WAVELET TRANSFORM FOR OPTICAL FLOW ESTIMATION ALGORITHM

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ABSTRACT

This paper described an algorithm for computing the optical flow (OF) vector of a moving objet in a video sequence based on geometric wavelet transform (GWT). This method tries to calculate the motion between two successive frames by using a GWT. It consists to project the OF vectors on a basis of geometric wavelet. Using GWT for OF estimation has been attracting much attention. This approach takes advantage of the geometric wavelet filter property and requires only two frames. This algorithm is fast and able to estimate the OF with a low-complexity. The technique is suitable for video compression, and can be used for stereo vision and image registration.

KEYWORDS

Geometric Wavelet, Curvelet Wavelet, Motion Estimation, Optical Flow

1. INTRODUCTION

Recherch work on optical flow estimation has previously been approved out to different applications which found in various fields such as signal and image processing; pattern recognition and computer vision, astronomy, acoustics and geophysics. It also finds place in medicine and meteorology by processing related images. Another area of high importance is the detection and tracking of moving targets in military applications [8],[9],[10] and [12].

A Great number of approaches for OF estimation have been proposed in the literature, including gradient-based, correlation-based, energy based, and phase based techniques [1].

The use of real wavelet in this approach suffers from two main problems; the lacks of shift invariance and poor directional selectivity. The geometric wavelet solves these problems and still desired to provide special characteristics.

The wavelet curvature is applicable principally in motion estimation edge detection and texture discrimination.

The rest of the paper is organized as follows. In Section 2, we introduce the principle and the description of the proposed algorithm. Section 3 shows the experimental performance of optical flow estimation. Finally, Section 4 concludes our contribution and merits of this work.

2. OPTICAL FLOW ESTIMATION ALGORITHM

2.1. Geometric Wavelet

Curvelet transform correspond on association of different steps: the application of filters pass-bands, on segmentation dyadic of each band frequency and transform Ridgelet on each zone segmented. The decomposition frequented associated on the dyadic segmentation permit conditioner the data for the Ridgelet transform with the aim of describe the singularities, where the size and the form of the motif variant. The description of the singularities where the size and the form of the motif variant. The description correspond the variability on the position: position associates on different dyadic zones.

The aim of this variant is permit the separation in the signal where the motif is very complex that in Ridgelet transform. This transform is very adapted for the split of a real image, it approximate the contour from an ensemble of segments. This transform ameliorant the singularities of an image, on the contrary, it is very redundant. It exists the alternatives for the limitation of the redundancy.

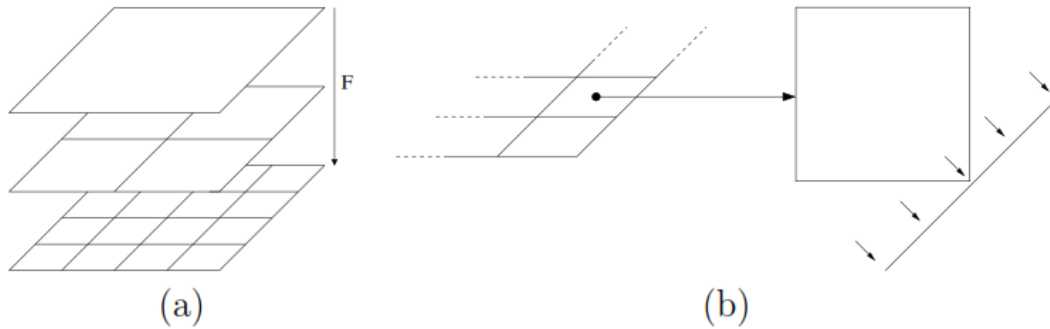


Figure (1): (a) Decomposition of an image with filter banc. (b) Application of Ridgelet transform in each zone dyadic.

2.2. Gradient Constraint

Our work shows that geometric wavelet transform technique seems more accurate in optical flow estimation.

This technique is based on the assumption of the gradient constraint. This equation can be expressed as

$$I(x + \Delta x, y + \Delta y, t + \Delta t) = I(x, y, t) + \frac{\partial I}{\partial x} \Delta x + \frac{\partial I}{\partial y} \Delta y + \frac{\partial I}{\partial t} \Delta t + H. O. T$$

$$\frac{\partial I}{\partial x} \Delta x + \frac{\partial I}{\partial y} \Delta y + \frac{\partial I}{\partial t} \Delta t = 0$$

Or

$$\frac{\partial I \Delta x}{\partial x \Delta x} + \frac{\partial I \Delta y}{\partial y \Delta t} + \frac{\partial I \Delta t}{\partial t \Delta t} = 0$$

Which result in:

$$\frac{\partial I}{\partial x} V_x + \frac{\partial I}{\partial y} V_y + \frac{\partial I}{\partial t} = 0$$

Thus:

$$I_x V_x + I_y V_y = -I_t$$

$$\nabla I^T \cdot \vec{V} = -I_t$$

Where V_x, V_y are the optical flow of $I(x, y, t)$ and $\frac{\partial I}{\partial x}, \frac{\partial I}{\partial y}$ and $\frac{\partial I}{\partial t}$ or I_x, I_y and I_t are the derivatives spatial and temporal of the image.

Our method introduces an additional condition for estimating the optical flow because it is an equation in two unknowns and cannot be solved as such. To discover the optical flow another set of equations is needed, given by some additional constraint.

2.3 Method

The framework of the algorithm is illustrated:

$$I_x \cdot f(X, Y) p = -I_t$$

$$f(X, Y) = \begin{bmatrix} \dots & \dots & \dots & \dots & \dots & \dots \\ x_i & y_i & 1 & 0 & 0 & 0 \\ 0 & 0 & 0 & x_i & y_i & 1 \\ \dots & \dots & \dots & \dots & \dots & \dots \end{bmatrix}^T,$$

Where

$$I_x = \begin{bmatrix} I_{x_1} & I_{y_1} & 0 & 0 & \dots & 0 & 0 \\ \vdots & \vdots & \vdots & \vdots & \ddots & 0 & 0 \\ 0 & 0 & 0 & 0 & \dots & I_{x_M} & I_{y_M} \end{bmatrix}$$

By applying the geometric wavelet transforms at the level l , we get the hierarchical gradient constraint functions (see figure 1).

$$A^l p = -I_t^l$$

The global equation of gradient constraint at all scale levels L is:

$$A p = b$$

$$A = [A^0, A^1, \dots, A^L] \quad b = -(I_t^0, I_t^1, \dots, I_t^L)^T$$

3 Experiment results:

In our experiments, we used three of sequences synthetic and four methods for comparison. For our simulation the low and high pass filter are done by

$$h_{low} = [-0.5 - j, 3 - 0.5j, -0.5 + j, 3 + 0.5j]$$

$$h_{high} = [-1.5 - j, 1 - 0.5j, -1.5 + j, 1 + 0.5j]$$

We evaluate the optical flow by using the angular error measurement between the correct velocity (u_c, v_c) and the estimate velocity (u_e, v_e) with 100% density, the average error and standard deviation were calculated.

Three images sequences were used to test our algorithm and compared with other optical flow technique:

$$\theta_{err} = \arccos\left(\frac{u_e u_c + v_e v_c + 1}{\sqrt{u_e^2 + v_e^2 + 1} \sqrt{u_c^2 + v_c^2 + 1}}\right)$$

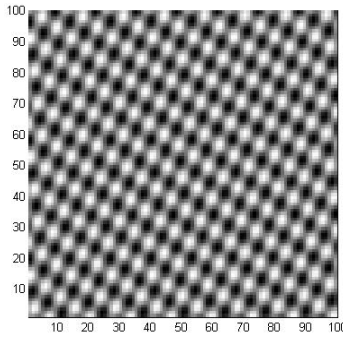


Figure 2.A. Sequence mysineB-6

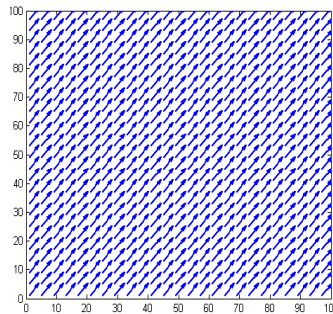


Figure 2.B. Optical Flow measuring by using real wavelet transforms

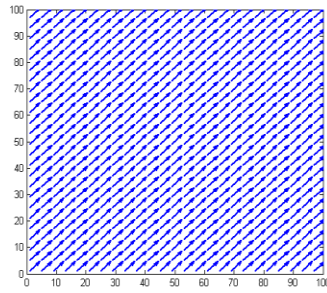


Figure 2C. Optical Flow measuring by using geometric wavelet transforms



Figure 3.A. Sequence Diverging tree

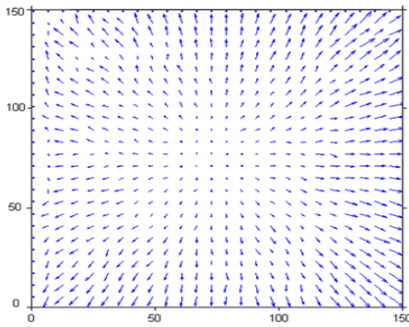


Figure 3.B. Optical Flow measuring by using real wavelet transforms

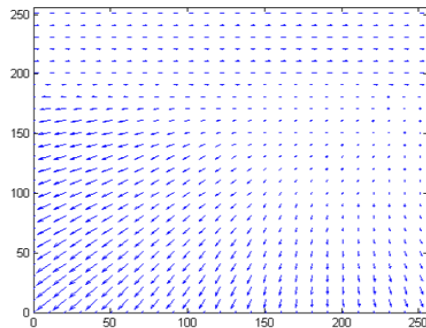


Figure 3C. Optical Flow measuring by using Geometric wavelet transforms

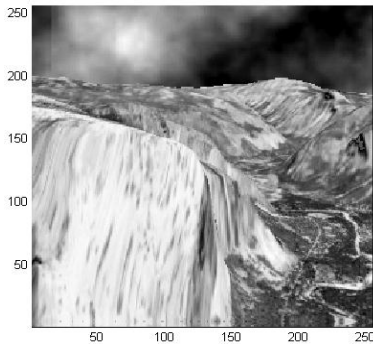


Figure 4.A. Sequence Yosemite

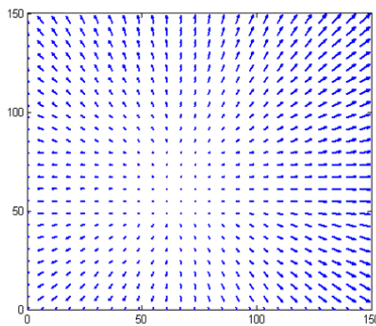


Figure 4.B. Optical Flow measuring by using real wavelet transforms

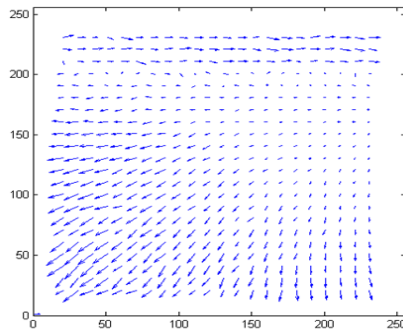


Figure 4C. Optical Flow measuring by using Geometric wavelet transforms

Table 1. Comparison of different methods of sequence “my sineB.6”.

Method	Images	Error	deviation	Density (%)
Motion estimation using complex wavelet	2	0.79°	0.68	100
Motion estimation using real wavelet	2	5.35°	4.56°	100
Horn et Schunk (original)	2	12.02°	11.72°	100
Horn et Schunk (modify)	7-13	2.55°	3.67°	100
Anandan	2	7.64°	4.96°	100
Singh	2	8.60°	4.78°	100

Table 2.Comparison of different methods of sequence “Diverging tree”.

Method	Images	Error	deviation	Density (%)
Motion estimation using complex wavelet	2	0.79°	0.68	100
Motion estimation using real wavelet	2	5.35°	4.56°	100
Horn et Schunk (original)	2	12.02°	11.72°	100
Horn et Schunk (modify)	7-13	2.55°	3.67°	100
Anandan	2	7.64°	4.96°	100
Singh	2	8.60°	4.78°	100

Table 3.Comparison of different methods of sequence “Yosemite”.

Method	Images	Error	deviation	Density (%)
Motion estimation using complex wavelet	2	4.52°	4.65°	100
Motion estimation using real wavelet	2	9.43°	8.87°	100
Horn et Schunk (original)	2	32.43°	30.28°	100
Horn et Schunk (modify)	7-13	11.26°	10.59°	100
Anandan	2	15.84°	13.46°	100
Singh	2	13.16°	12.07°	100

4. Conclusion

The algorithm estimate the OF by resolving the resulted equations from the projection of the gradient constraint in the Geometric wavelet bases. The experimental results demonstrate that the

Geometric wavelet is capable to estimate many kinds of movement. Testing on synthetic data sets has shown good performance compared par real wavelet.

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