ISO9126 Based Software Quality Evaluation Using Choquet Integral

Abdelkareem M. Alashqar¹, Ahmad Abo Elfetouh² and Hazem M. El-Bakry³

¹,²,³Information Systems Dept., Faculty of Computer and Information Sciences, Mansoura University, EGYPT

ABSTRACT

Evaluating software quality is an important and essential issue in the development process because it helps to deliver a competitive software product. A decision of selecting the best software based on quality attributes is a type of multi-criteria decision-making (MCDM) processes where interactions among criteria should be considered. This paper presents and develops quantitative evaluations by considering interactions among criteria in the MCDM problems. The aggregator methods such as Arithmetic Mean (AM) and Weighted Arithmetic Mean (WAM) are introduced, described and compared to Choquet Integral (CI) approach which is a type of fuzzy measure used as a new method for MCDM. The comparisons are shown by evaluating and ranking software alternatives based on six main quality attributes as identified by the ISO 9126-1 standard. The evaluation experiments depend on real data collected from case studies.

KEYWORDS


1. INTRODUCTION

Software quality is an important and essential issue especially in current rapid change in the software development industry. The process of evaluating software quality offers various benefits during the development process as it let developers to deliver high qualified software product. Quality is a relative term which differs with viewpoints transcendental view, product view, manufacturing view, user view and value-based View [17]. Several models have been proposed like ISO/IEC 9126 Model [16], McCall model [20], Boehm model [6], FURPS model [15], Dromey [9] model, and FURPS model [14], to evaluate generic software application. A comparative study of software quality models is found in [1] [26] [31]. Quality models define software product qualities as a hierarchy of factors, criteria and metrics. A quality factor represents behavioral characteristics of the system; a quality criterion is an attribute of a quality factor that is related to software production and design; while a quality metrics is a measure that captures some aspect of a quality criterion [32]. Most of the works that focus on software quality evaluation do not reference the aggregation methods used to calculate the values of the different element of the model. Sometimes a simple weighted average is used to summaries the various quality measurements into a single score as proposed in [3] and [23]. Over the past decade, fuzzy decision support has emerged as a means of providing effective tools and techniques for solving MCDM problems. The authors in [11] used the aggregation function, a fuzzy decision-support technique, to support the MCDM process in a game theory context. An MCDM approach based on ordered weighted averaging (OWA) operators was proposed in [8] which permits a...
sophisticated aggregation of measured atomic quality values using linguistic criteria to express human expert’s evaluations. Recent studies as in [21] and [32], also adopts MCDM approach based on fuzzy measures to evaluate software quality. In this study, we introduce a relatively fuzzy decision support technique based on an aggregation function named the Choquet Integral (CI) into the MCDM problem of evaluating quality of e-learning websites. The evaluation depend on the main quality attributes defined in ISO/IEC 9126 standard, and take into account the interactions between these quality attributes. In addition to that, the evaluations utilize real empirical data collected from previous studies.

The rest of this paper in organized as follows: Section 2 mentions related work. Section 3 explains the proposed method that emphasizes the aggregations methods especially CI. Section 4 presents the experimental results, and Section 5 provides the conclusion and future work.

2. RELATED WORK

Some research studies attempt to evaluate software quality using fuzzy multi criteria approach without considering interaction between criteria as [7] [29] and [30]. The work in [7] provides a method to estimate the software quality criteria using fuzzy multi criteria approach. The method used to quantify software quality for generic applications. The authors in [29] proposed a MCDM approach to software quality assessment using fuzzy measures to model software experts’ decision making processes and help them to predict/evaluate software quality. Their approach helps to predict/evaluate software quality with consistently over 60% accuracy. While the authors in [30] present a software quality prediction model based on a fuzzy neural network. The proposed model is a hybrid model of Artificial Neural Network (ANN) and Fuzzy Logic (FL), which exploits the advantages of ANN and FL while eliminating their limitations.

A limited number of attempts apply fuzzy measure techniques to the modeling of MCDM process in evaluating software quality attributes considering the interaction between these quality attributes. In an early study carried out by [32], presents a fuzzy integral approach as an aggregation operator to produce the overall assessment of quality attributes for web-based applications (WBA). Later work [22] proposes a methodology based on fuzzy measure using CI for comparing different software solutions based on the software requirements specification (SRS) to a common problem. Our work is closest to work done in [22] [32] which use CI with fuzzy measure to quantify the interacting software quality parameters and finds the best software among different software and also made analysis of effect of interaction among criteria in finding best alternative. However, it is different in that it uses CI to evaluate specific type of software that is e-learning websites from user perspective depending on empirical collected data from previous studies. Furthermore, our evaluations are based on ISO/IEC 9126 quality model. Furthermore, while [22] assigned different values to $\xi$ (an interaction degree among criteria as proposed by [27]) to show how it affects the evaluation results, we use real interaction values as stated in the literature in our evaluation purposes.

3. RESEARCH METHOD

This section presents a description of an aggregation function that is widely used by researchers in quantitative evaluations, followed by a description of fuzzy measure method using CI as a new approach for evaluation.
3.1 Aggregation Function

MCDM is used if there are a set of alternatives and each is evaluated against several criteria. For example, if a user wants to select the best one of several developed websites, it needs to consider the best usability, the best efficiency, and so on. The degree to which an alternative satisfies a criterion corresponds to a utility value [28]. The scores must then be combined in some ways to produce an overall rating for that alternative. Such a process is very similar to an aggregation function or aggregation operator, which combines several inputs into a single representative output. The averaging aggregation is one of the most widely used type of aggregation functions.

The term “average” is commonly employed in everyday language when referring to the arithmetic mean (AM). The AM of $n$ values is the function:

$$\text{AM}(x) = \frac{1}{n} \left( x_1 + x_2 + \cdots + x_n \right) = \frac{1}{n} \sum_{i=1}^{n} w_i x_i$$

(1)

For example for a given input $x = (0.5, 0.2, 0.7)$, the AM is $(0.5 + 0.2 + 0.7)/3 = 0.47$.

In case some criteria are considered as more important than others, it is common to consider the aggregation function to be additive and to take the form of a weighted arithmetic mean (WAM). WAM is a linear function with respect to a positive valued weighting vector $w$ with $\sum_{i=1}^{n} w_i = 1$:

$$WAM_w(x) = w_1 x_1 + w_2 x_2 + \cdots + w_n x_n = \sum_{i=1}^{n} w_i x_i$$

(2)

For example if a given input $x = (0.5, 0.2, 0.7)$ has corresponding weights $w = (0.5, 0.3, 0.2)$, then the $WAM_w(x) = 0.5(0.5) + 0.2(0.3) + 0.7(0.2) = 0.25 + 0.06 + 0.14 = 0.45$.

Although the most often used aggregation operators are the WAM [19], it is not an appropriate method when there is an interaction among the criteria. Therefore, we choose CI aggregation function as a type of fuzzy measure that takes into account the interaction among criteria [28].

3.2 Fuzzy Measures and Choquet Integral

A fuzzy measure (also called a capacity) $\mu$ on a set of input criteria $X = \{x_1, x_2, \ldots, x_n\}$ is a set function $\mu: 2^X \rightarrow [0,1]$ satisfying [12][28]:

(i) $\mu(\emptyset) = 0$ and $\mu(X) = 1$ (boundary conditions).
(ii) $A, B \subseteq X, A \subseteq B$ implies $\mu(A) \leq \mu(B)$ (monotonicity).

Furthermore a capacity $\mu$ on $X$ is said to be [12] :

- Additive if $\mu(A \cup B) = \mu(A) + \mu(B)$ for all disjoint sunsets $A, B \subseteq X$, and
- Cardinality-based if, for any $B \subseteq X, \mu(B)$ depends only on the cardinality of $B$.

Note that there is only one capacity on $X$ that is both additive and cardinality-based. It is called the uniform capacity and denote it by $\mu^*$. It is easy to verify that $\mu^*$ is given by

$$\mu^*(B) = \frac{b}{X}, \forall B \subseteq X$$

In the framework of aggregation, for each subset of criteria $A \subseteq X$, the number $\mu(A)$ can be interpreted as the weight or the importance of $A$. The monotonicity of $\mu$ means that the weight of
a subset of criteria cannot decrease when new criteria are added to it. In the case \( X = \{x_1, x_2, x_3\} \) the representation of fuzzy measures is shown as:

\[
\begin{align*}
\mu(\emptyset) & \\
\mu(1) & \\
\mu(2) & \\
\mu(3) & \\
\mu(1,2) & \\
\mu(1,3) & \\
\mu(2,3) & \\
\mu(1,2,3) & 
\end{align*}
\]

The discrete CI with respect to a fuzzy measure \( \mu \) is given by:

\[
CI_\mu(x) = \sum_{i=1}^{n} x_{(i)} \left[ \mu(\{j \mid x_j \geq x_{(i)}\}) - \mu(\{j \mid x_j \geq x_{(i+1)}\}) \right]
\]

(3)

Where \( x_{(1)}, x_{(2)}, \ldots, x_{(n)} \) is a non-decreasing permutation of the input \( x \), and \( x_{(n+1)} = \infty \) by convention. For example, given an input \( x = (0.5, 0.2, 0.7) \) and the fuzzy measure values:

\[
\begin{align*}
\mu(\emptyset) & = 0 \\
\mu(1) & = 0.5 \\
\mu(2) & = 0.3 \\
\mu(3) & = 0.2 \\
\mu(1,2) & = 0.7 \\
\mu(1,3) & = 0.6 \\
\mu(2,3) & = 0.9 \\
\mu(1,2,3) & = 1
\end{align*}
\]

To calculate the CI, the input \( x \) is arranged in a non-decreasing \((0.2, 0.5, 0.7)\). Then, the result obtained from the input \( x \) is:

\[
CI_\mu(x) = 0.2[\mu(1,2,3) - \mu(1,3)] + 0.5[\mu(1,3) - \mu(3)] + 0.7[\mu(3)]
\]

\[
= 0.2(1 - 0.6) + 0.5(0.6 - 0.2) + 0.7(0.2)
\]

\[
= 0.2(0.4) + 0.5(0.4) + 0.7(0.2) = 0.42
\]

The result value falls between the maximum and the minimum input expected in the bounding condition of averaging functions such as AM.

It should be noted we adopted the additive fuzzy measure in this paper. A fuzzy measure is called additive if \( \mu(A \cup B) = \mu(A) + \mu(B) \) whenever \( A \cap B = \emptyset \), super additive if \( (A \cup B) \geq (A \cap B) \) and sub additive if \( (A \cup B) \leq (A \cap B) \) whenever \( A \cap B = \emptyset \).

Fuzzy measures are rich and important family. Furthermore, when they are used with some of the integrals such as CI, they can generalize some well-known aggregation operators such as the AM. The CI corresponds to the WAM functions when it is defined by the additive fuzzy measures. We also adopted a \( k \)-additive as a recently concept developed by [10] to reduce the complexity in fuzzy measure. The interactions between criteria are only considered for subsets of \( k \) elements or less, which reduces the number of variables to define the fuzzy measure. It allows for a trade-off between modeling ability and complexity. A decision maker can decide how complex a fuzzy

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measure that he wishes to consider by selecting a k-additive value \((1 \leq k \leq n)\). When \(k = 1\) the CI becomes equivalent to WAM, and when \(k = n\) the fuzzy measures are said to be unrestricted.

The Shapley value is an important concept related to CI used to measure the overall importance of each criterion alone in all coalitions. Let \(\mu\) be a fuzzy measure and \(X = \{x_1, x_2, \ldots, x_n\}\) be the set of criteria. The Shapley index for every input \(x_i \in X\) is defined as:

\[
\phi_{\mu}(i) = \sum_{A \subseteq X / \{x_i\}} \frac{(n-|A|-1)!|A|!}{n!} [\mu(A \cup \{x_i\}) - \mu(A)]
\]

The Shapley value is the vector \(\phi_{\mu}(v) = \phi_1, \phi_2, \ldots, \phi_n\). The index \(\phi_i\) can be interpreted as a kind of average value of the contribution of criteria \(x_i\) in all groups of criteria. It also represents a true sharing of the total amount \(\mu(X)\) as it must satisfy the condition \(\sum_{i=1}^{n} \phi_{\mu}(i) = 1\).

A powerful capability of fuzzy measure approach using CI is the consideration of criteria interaction. The interaction indices are interpreted as the behaviors of criteria in groups or as a measurement of the interaction among criteria in the decision-making process. If \(X = \{x_1, x_2, \ldots, x_n\}\) is the set of criteria, then the interaction index for every set \(\subseteq X\):

\[
I_{\mu}(A) = \sum_{B \subseteq X / A} \frac{(n-|A|-|B|)!|B|!}{(n-|A|+1)!} \sum_{C \subseteq A} (-1)^{|A/C|} \mu(B \cup C)
\]

This measure can include all combinations of groups of criteria where \(I_{\mu}(A) \in [-1,1]\). The interaction index \(I_{\mu}(ij)\) for each pair \(A = \{x_i, x_j\}\) of criteria is usually used due to its convenience of interpretation. For a pair of criteria \(x_i\) and \(x_j\), if they have a positive interaction (complement), then \(I_{\mu}(ij) > 0\). Similarly, if \(x_i\) and \(x_j\) have a negative interaction (correlation), then \(I_{\mu}(ij) < 0\). When \(x_i\) and \(x_j\) have little or no interaction (independence), \(I_{\mu}(ij) = 0\). The \(I_{\mu}(ij)\) is more than just the interaction between a pair of criteria themselves because each pair is considered in the presence of all groups.

### 3.3 A Comparison between WAM and CI

In the WAM aggregation method seen so far, only a single weight is considered for each data element. Besides, we cannot consider how to measure the importance of a set of sources. For example, in the case of the multi-criteria decision making problem of website evaluation, we can state that the efficiency criterion has an importance of 0.3, and that usability is more important, and thus, its weight is 0.5. However, we have not considered the importance of efficiency and usability when considered together. Fuzzy measures permit us to incorporate considerations not included in the weights for the WAM operator. In particular, they can be used to express redundancy, complementariness, and interactions among information sources or criteria.

Therefore, tools that use fuzzy measures such as CI to represent background knowledge permit the consideration of sources that are not independent. We can see that the advantage of CI lies in the fact that the fuzzy measure can account for the importance and the interaction between every subset of criteria [28].

Lest us consider a decision maker of an organization has to evaluate the software products according to their level in functionality (F), usability (U), and efficiency (E). Suppose that the organization put more importance in functionality and usability than efficiency and the assigned weights could be for example 0.4, 0.4, and 0.2 respectively. Applying WAM, Product A is better than Product B and Product C, since it has highest weighted score as shown in Table 1 although it was weak in characteristic E. However if the organization wants the product that is well versed
with all the three characteristics then Product C is better than other products as it has scored consistent scores in all the three characteristics. This is due to much importance is given to characteristics F and U, which are in sense synergic. So this problem can be solved using CI with fuzzy measure as input. As F and U are synergic characteristics, the weights used for the pair characteristics F and U should be less than the sum of weights of characteristics F and U, and hence the sum of weights of characteristics F and U, \( \mu(F, U) = 0.5 \). As product equally good at F and E characteristics must be favored so that the weights for the pair of F and E must be greater than sum of individual weights of F and E, so \( \mu(F, E) = \mu(U, E) = 0.9 \), where \( \mu(F, U, E) = 1.0 \). So according to CI approach Product C is better than Product A and B as it has highest CI value shown in Table 1. In contrast to WAM score Product A was better than B and C. Therefore it can be concluded that fuzzy measure using CI is a better approach than WAM because it takes into account interaction and importance of each criterion.

<table>
<thead>
<tr>
<th>Product</th>
<th>F</th>
<th>U</th>
<th>E</th>
<th>WAM</th>
<th>CI</th>
</tr>
</thead>
<tbody>
<tr>
<td>Product A</td>
<td>9</td>
<td>8</td>
<td>5</td>
<td>7.8</td>
<td>6.9</td>
</tr>
<tr>
<td>Product B</td>
<td>4</td>
<td>6</td>
<td>8</td>
<td>6</td>
<td>6.3</td>
</tr>
<tr>
<td>Product C</td>
<td>7</td>
<td>7</td>
<td>8</td>
<td>7.2</td>
<td>7.9</td>
</tr>
</tbody>
</table>

We used the application of the Kappalab R package [13]. Kappalab package includes implementation of several methods for fuzzy measures (called capacity) identification in Choquet integral based multi-attribute utility theory (MAUT). These methods are based on least-squares based approaches, maximum split approach, minimum variance approach and minimum distance approaches. Most of the methods for capacity identification proposed in the literature can be stated as optimization problems. However, they differ according to their objective function and the preferential information they require as input [12]. We developed a tool using RStudio [24] that utilize these methods. The main parameters values used as input to the kappalab R package methods are the number of criteria and their weights, the alternative instances, the interaction indices and the k-additive. There are six criteria which represent the ISO/IEC9126 based six quality attributes. The instances of alternatives as well as the criteria weights are collected depending on empirical data from two previous case studies. These studies provide evaluation of e-learning websites where each case includes five instances. The criteria weights and the interaction indices are identified depending on industry experience. The k-additive value corresponds to the number of selected criteria.

4. Experiments and Results

The data used in this paper were collected from two separate previous case studies that provide evaluations for e-learning websites from the student perspective (see [23] and [3]). The evaluations in the first one (which we called Case 1) were carried out in Thailand universities, and evaluations presented in the later one (which we called Case 2) were carried out in Jordan universities. Each study provides evaluations of five different categories of e-learning websites using traditional averaging methods. However the names and categories are different in both studies. The categories in Case 1 are: Educational and Social Science, Humanities, Agriculture, Science and Technology, and Business Administration, where we call them A1, A2, A3, A4 and A5 respectively. The categories in Case 2 are: Arts, Business, Educational and Social Sciences, Engineering and Science where we call them A1, A2, A3, A4 and A5 respectively.
In this paper we use the data described so far in evaluating e-learning websites based on ISO9126 quality attributes using CI approach. The data are shown in Table 2 and Table 3. Where ‘F’, ‘R’, ‘U’, ‘E’, ‘M’, and ‘P’ stand for “Functionality”, “Reliability”, “Usability”, “Efficiency”, “Maintainability”, and “Portability”, respectively.

Table 2: Case 1- Total quality attributes evaluations for 5 groups of subjects found in [23]

<table>
<thead>
<tr>
<th>QA</th>
<th>A1</th>
<th>A2</th>
<th>A3</th>
<th>A4</th>
<th>A5</th>
</tr>
</thead>
<tbody>
<tr>
<td>F</td>
<td>60.46</td>
<td>49.44</td>
<td>57.66</td>
<td>54.13</td>
<td>53.98</td>
</tr>
<tr>
<td>R</td>
<td>82.76</td>
<td>80.09</td>
<td>74.60</td>
<td>76.11</td>
<td>83.27</td>
</tr>
<tr>
<td>U</td>
<td>68.86</td>
<td>63.26</td>
<td>64.41</td>
<td>56.64</td>
<td>62.72</td>
</tr>
<tr>
<td>E</td>
<td>37.72</td>
<td>40.13</td>
<td>44.08</td>
<td>36.01</td>
<td>42.88</td>
</tr>
<tr>
<td>M</td>
<td>36.03</td>
<td>17.75</td>
<td>19.96</td>
<td>38.16</td>
<td>19.54</td>
</tr>
<tr>
<td>P</td>
<td>40.08</td>
<td>34.91</td>
<td>37.49</td>
<td>39.95</td>
<td>36.24</td>
</tr>
<tr>
<td>AM</td>
<td>54.47</td>
<td>47.60</td>
<td>49.70</td>
<td>50.17</td>
<td>49.78</td>
</tr>
</tbody>
</table>

Table 2: Case 2- Total quality attributes evaluations for 5 groups of subjects found in [3]

<table>
<thead>
<tr>
<th>QA</th>
<th>A1</th>
<th>A2</th>
<th>A3</th>
<th>A4</th>
<th>A5</th>
</tr>
</thead>
<tbody>
<tr>
<td>F</td>
<td>71.67</td>
<td>76.04</td>
<td>74.69</td>
<td>67.81</td>
<td>72.19</td>
</tr>
<tr>
<td>R</td>
<td>55.83</td>
<td>58.33</td>
<td>56.67</td>
<td>54.17</td>
<td>57.92</td>
</tr>
<tr>
<td>U</td>
<td>72.19</td>
<td>67.6</td>
<td>71.46</td>
<td>67.4</td>
<td>68.96</td>
</tr>
<tr>
<td>E</td>
<td>63.33</td>
<td>63.33</td>
<td>63.33</td>
<td>54.17</td>
<td>61.25</td>
</tr>
<tr>
<td>M</td>
<td>70.21</td>
<td>67.5</td>
<td>73.44</td>
<td>67.71</td>
<td>68.75</td>
</tr>
<tr>
<td>P</td>
<td>66.67</td>
<td>67.08</td>
<td>64.17</td>
<td>58.75</td>
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<td>AM</td>
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<td>67.29</td>
<td>61.67</td>
<td>64.98</td>
</tr>
</tbody>
</table>

Software quality is a relative term which differs with viewpoints. So different perspectives of quality can be considered; such as user view, developer view, manager view, etc. For example, from the system user’s point of view, usability of the system is the most important one; while from the viewpoints of developers and maintainers, maintainability is the most important one. In addition to that, the overall quality of software product can be expressed by a combination of different views. However, it must be taken into account that no software product can satisfy all of the stakeholders’ needs at the same time. In our work, the users’ viewpoint will be considered.

Given the fact that there are some trade-offs between software product capabilities and it is not possible to satisfy all of the software requirements at the same time, it is essential to determine the weights of all quality aspects in any software product. Because of the absence of relative importance of quality attributes represented by weights in the two mentioned previous case studies, the quality attributes weights were adopted from [5] as a result of industrial experience and experts refinement. We depend on these results on evaluating the e-learning websites. The weights are: 0.3, 0.19, 0.24, 0.18, 0.05, 0.04 as user’s view weights for “Functionality”, “Reliability”, ”Usability”, “Efficiency”, “Maintainability”, and “Portability”, respectively.

The relationships between quality attributes exist. Software products quality attributes are among the important subjects that require trade-offs especially when facing conflicts in quality requirements or customers’ desires and in order to conduct a correct and a successful tradeoff a rigorous analysis might be required [2]. The interaction between quality attributes is defined form [2] and [33] as depicted in Table 4 which shows 15 relationships for each pair of the 6 quality attributes.
Table 4: Quality attributes Relationships as identified in [2] and [28]

<table>
<thead>
<tr>
<th>QA</th>
<th>F</th>
<th>R</th>
<th>U</th>
<th>E</th>
<th>M</th>
</tr>
</thead>
<tbody>
<tr>
<td>R</td>
<td>+</td>
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<tr>
<td>U</td>
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<td>0</td>
<td>-</td>
<td>+</td>
</tr>
</tbody>
</table>

Where positive relationship means there is a synergy between the two quality attributes; in other words good values of one attribute result in a good value of the other. And the relationship means there is a conflict between the two quality attributes; in other words, a good value of one attribute result in a bad value of the other. The synergic relationship represented as complementary relationship in kappalab R package while the conflict relationship represented as substitutive relationship.

For calculating CI values we used the minimum distance (MD) approach because it helps in finding, if it exits, the closest capacity to a capacity defined by the decision maker (DM) and compatible with his/her initial preferences. This initial capacity is typically an additive capacity representing the DM’s prior idea of what the aggregation function should be. In the absence of clear requirements a very natural choice for fuzzy measure $\mu$ is the uniform capacity $\mu'$. Also we apply CI with less restricted fuzzy measures where the overall performance of CI increased as $k$ increased, and it achieved the best performance when $k$ is equal to the number of criteria where the number of criteria in our study is 6. In addition to that the use of the CI with less restricted fuzzy measures can model the MCDM process in a way that is closer to reality [18].

Table 5: Quality Attributes Evaluations for the 5 groups of subjects of case 1 obtained from WAM and CI

<table>
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<td>47.60</td>
<td>49.70</td>
<td>50.17</td>
<td>49.78</td>
</tr>
<tr>
<td>WAM</td>
<td>60.58</td>
<td>54.74</td>
<td>57.36</td>
<td>54.28</td>
<td>57.21</td>
</tr>
<tr>
<td>CI</td>
<td>57.25</td>
<td>52.57</td>
<td>53.98</td>
<td>52.16</td>
<td>54.45</td>
</tr>
</tbody>
</table>
Table 6: Quality Attributes Evaluations for the 5 groups of subjects of Case 2 obtained from WAM and CI

<table>
<thead>
<tr>
<th>QA</th>
<th>A1</th>
<th>A2</th>
<th>A3</th>
<th>A4</th>
<th>A5</th>
</tr>
</thead>
<tbody>
<tr>
<td>F</td>
<td>71.67</td>
<td>76.04</td>
<td>74.69</td>
<td>67.81</td>
<td>72.19</td>
</tr>
<tr>
<td>R</td>
<td>55.83</td>
<td>58.33</td>
<td>56.67</td>
<td>54.17</td>
<td>57.92</td>
</tr>
<tr>
<td>U</td>
<td>72.19</td>
<td>67.6</td>
<td>71.46</td>
<td>67.4</td>
<td>68.96</td>
</tr>
<tr>
<td>E</td>
<td>63.33</td>
<td>63.33</td>
<td>63.33</td>
<td>54.17</td>
<td>61.25</td>
</tr>
<tr>
<td>M</td>
<td>70.21</td>
<td>67.5</td>
<td>73.44</td>
<td>67.71</td>
<td>68.75</td>
</tr>
<tr>
<td>P</td>
<td>66.67</td>
<td>67.08</td>
<td>64.17</td>
<td>58.75</td>
<td>60.83</td>
</tr>
<tr>
<td>AM</td>
<td>66.65</td>
<td>66.65</td>
<td>67.29</td>
<td>61.67</td>
<td>64.98</td>
</tr>
<tr>
<td>WAM</td>
<td>67.01</td>
<td>67.58</td>
<td>67.96</td>
<td>62.30</td>
<td>66.11</td>
</tr>
<tr>
<td>CI</td>
<td>65.90</td>
<td>67.35</td>
<td>66.92</td>
<td>61.79</td>
<td>65.58</td>
</tr>
</tbody>
</table>

Studying the results in Table 5 for Case 1, obtained by considering the Shapley values and considering synergic and conflicts element with CI, can let us report that the rank of websites as follows A1>A5>A3>A2>A4, which means that A1 followed by A5 outperform the other alternatives, while the rank using WAM is A1>A3>A5>A2>A4.

And studying the results in Table 6 for Case 2, obtained by considering the Shapley values and considering synergic and conflicts element with CI, can let us report that the rank of websites as follows A2>A3>A1>A5>A4, while the rank using WAM is A3>A2>A1>A5>A4.

It is important to mention here that we compared the evaluation results of fuzzy measure using CI to WAM only, because these methods take into account the weighting of criteria, while AM does not consider this.

5. CONCLUSION AND FUTURE WORK

Evaluating software quality is always an interest of researchers working to support users and developers in decision making. Traditional methods as AM and WAM are unable to explore MCDM process completely and accurately. In this paper we introduce a fuzzy measure technique that uses the CI approach in evaluating quality attributes of e-learning websites based on ISO/IEC 9126 and depending on real data by analyzing the Shapley values and the interaction between criteria. The results show more convenient evaluation for users and developers in decision making. The calculation results conducted on two example case studies in Section 4 illustrate that using CI approach with the consideration of synergic and conflict elements can essentially change the alternatives ranking.

Extension to this work include taking into account evaluating sub-criteria of quality attributes and considering different software product views. Carrying out the experiments using large amount of empirical data is also needed to refine the results. Furthermore, it is needed to develop a tool that facilitates applying experiments emphasizing the approaches provided by Kappalab R package.

REFERENCES


