BOUND ANT COLONY ALGORITHM FOR TASK ALLOCATION ON A NETWORK OF HOMOGENEOUS PROCESSORS USING A PRIMARY SITE (BTS-ACO)

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ABSTRACT

Efficient scheduling of tasks for an application is considered a crucial aspect in distributed systems to achieve a superior performance. This paper presents a task scheduling algorithm based on the Ant Colony Optimization (BTS-ACO). This algorithm depends on an initial bound on each processor to control the procedure of task allocation. Herein, the priority of tasks is to processor with the minimal load. The algorithm investigates the effect of scheduling sorted (SLoT) and random (RLoT) list of tasks. The performance of the algorithm is demonstrated by the time taken for producing effective schedules, makespan of the schedule, and load balance of the models. The results show that BTS-ACO solution with sorted list has better performance than random list.

KEYWORDS

Ant colony optimization Task scheduling, parallel programming, load balancing, Makespan

1. INTRODUCTION

The problem of parallel processing in distributed and computers cluster systems is continuing to gain big interest. A parallel program is a program that can be divided into a collection of subtasks. These subtasks are usually called tasks or processes [1]. Some of tasks depend on the completion of other tasks; others can be executed at the same time, which increases parallelism of the problem. Tasks can be executed in sequence or at the same time on one or more processors. A computer cluster consists of multiple computers that are linked through a LAN. The networked computers essentially act as a single, much more powerful machine. A computer cluster offers faster processing speed, larger storage capacity, better data integrity and the ability to handle large computational load [2]. When a cluster is built, usually one computer is chosen as a root or primary node. The responsibility of the root is to receive a task, divide it into subtasks, then delivers these subtasks to the cluster members. The root continuous to communicate with the nodes in the cluster. When the nodes finish executing their share, they send the result back to the root which will integrate them into its final form.

Task scheduling is the problem of assigning tasks to the processors in the system in a manner that will minimize the makespan, while assuring the correctness of the result. Makespan is the completion time of the last task relative to the start time of the first task. The scheduling problem is a NP-hard problem[3] and it is not trivial. Many task scheduling algorithms have been
presented. The objectives of these algorithms are usually to balance the load among processors, reduce the execution time of the parallel program, minimize the makespan and others.

Task scheduling algorithms can be static or dynamic approaches. Static or off-line scheduling algorithms assume that all information about the scheduling problem is known in advance, and the solution to the problem is computed and found before the system starts running. On the other hand, dynamic or on-line scheduling algorithms compute the solution for tasks while the scheduling process is running. Dynamic scheduling is flexible and can cope with any unexpected changes in the system during the scheduling process.

Many methods of scheduling techniques exist. These methods can be classified into three categories; graph theory based methods [4], mathematical models based methods [5], and heuristic techniques [6][7][8][9]. Several numbers of heuristics have been used and the most well-known of them are; the iterative improvement algorithms, the probabilistic optimization algorithms, and the constructive heuristics.

Ant colony algorithms are meta-heuristic algorithms inspired by the behavior of real ant colonies. Real ants find food sources by indirectly communicating together by means of releasing certain amount of pheromones while walking.

Ants follow paths with higher amount of pheromones. These paths are usually the optimal solutions. The ant colony algorithm is applied to solve many difficult optimization problems in different applications [10][11][12][13][14][15][16]. In this paper we apply a modified version of ant colony algorithm to task scheduling in a computer cluster system. Simulation of the proposed algorithm is presented. The simulator defines the different parameters of the system such as execution time of tasks, the criteria of a scheduler, etc. Finally, the paper compares the performance of various task scheduling approaches.

The rest of the paper is organized as follows. In section 2, the related work is presented. Section 3 discusses the problem statement. Section 4 describes the methodology and design, and briefly illustrates how to implement a task scheduling system using an Ant Colony Optimization (ACO) algorithm. Section 5 presents the experimental results and the discussions. Section 6 concludes the paper and proposes future work for the problem.

2. RELATED WORK

Task scheduling is an NP-problem. Many task scheduling algorithms have been presented. These methods can be classified into three categories; graph theory methods, mathematical methods, and heuristic techniques. Some of the heuristic algorithms are min-min [17], the fast greedy [17] and Ant colony algorithms [18]. In min-min method, the task with minimum completion time is selected first and assigned to a processor. This algorithm has fast scheduling time, but poor load balancing [19][20]. Fast Greedy assigns each task, in arbitrary order, to the processor with the minimum completion time [19]. Some algorithms force some conditions to improve the performance such as in [21], where the task can be moved from one machine to another. This action improves the load balancing, but on the other hand the traffic in the system is increased.

3. PROBLEM STATEMENT

The system consists of a cluster of m processing machines connected via a network. Let 
P = {P1, P2... Pk} denote the set of processors in the system. All processors in the cluster are fully connected. The processors in the cluster are homogeneous, meaning that the execution time
of a specific task is the same on any processor. One of the processors in the cluster is chosen as a root. The function of the root is to divide the original task into independent subtasks. After these subtasks are delivered to the processors in the cluster and executed, the results are sent back to the root which integrates them into their final format [1].

The Tasks Set \( T = \{T_1, T_2, \ldots, T_n\} \) has \( n \) tasks. The set \( T \) stores the execution time of the tasks to be schedules. The number of processors in the system is less than the number of tasks. So each processor will probably have more than one task. The number of tasks assigned to a processor will depend on the execution time of the tasks and on the load already assigned to that CPU. Each processor should wait for some time before it can execute its subtask. This is the time needed to transmit the task over the communication channel. Usually the execution time of the subtask is much higher than its transmission time, so we will neglect the transmission time in our calculations.

All processors involved in the computing process of the parallel tasks must stop at the same time to obtain the minimum finish time. This optimality criterion has been rigorously proved in the literature [22]. The goal is to minimize the maximum total processing time, also known as the makespan, on any processor. So if we have \( K \) processors in the system, then \( E_{T_1} = E_{T_2} = \ldots = E_{T_K} \), where \( (E_{T_i}) \) is the total execution time of processor \( i \) [2].

An upper bound value is used to control the scheduling of tasks over the processors. This value is unique for the system. Each time a task is delivered to a processor, the total execution times of all tasks \( (E_{T_i}) \) assigned to processor \( I \) (including the new task) is tested against the bound. If \( E_{T_i} \) exceeds the bound, then the task will be sent to another processor. The value of the bound is calculated using equation 1 below. \( m \), in the equation, is the number of tasks to be scheduled, and \( k \) is the number of processors in the cluster.

\[
Bound = \frac{\sum_{j=0}^{j=m} T_j}{k}
\]

Equation 1

The bound can be increased during the scheduling processor. This action is done in case there is a task that can’t be delivered to any processor because the load of each processor plus the new task exceeds the bound.

At the end of the scheduling process the finish time of each processor is examined. The ant colony algorithm is used to departure tasks to CPUs in the system. Our goal is to make an equal finish time for all processors. Unfortunately, this will be difficult since each task have different execution time.

As mentioned above, this paper proposed different approaches in which tasks were stored and picked from the array in order to be delivered to the processors.

**Case A: Random List of Tasks (RLoT)**

With this policy, a task is picked randomly from the array and sent to a processor. This policy is the simplest to implement since it involves only a negligible amount of overhead when generating the tasks.
Case B: Sorted List of Tasks (SLoT)

In this case the tasks in the array T are sorted in descending order, according to their execution time, and picked in sequence. Unfortunately, extra computational time will be needed for sorting the array. Each time a task is picked and delivered to a different processor. Since we have a sorted task list, the first k tasks with higher execution times will be picked first, and then the next k tasks with lower execution times will be picked, and so on. Using this method we assign the processor's tasks with high and small execution times in an attempt to balance the load given to these processors. The ant colony algorithm will benefit from this technique in setting initial pheromone values between small and big ones. This will help in building schedules faster and achieving a higher degree of load balancing.

4. Ant Colony Optimization for Tasks Scheduling

Task scheduling problem is represented as a complete graph $G = (V, E)$ where node $(V)$ represents a task and the edge $(E)$ represents a path between two tasks. Each edge in the graph is assigned a pheromone trial $t$. An illustrative example is depicted in Figure 1.

![Full Task Set = \{t1,t2,t3,t4,t5,t6\}, Two processors. Allocate \{t1,t2,t5\} to processor 1, And allocate \{t3,t4,t6\} to processor 2, where number of processor equal 2](Image)

**Figure 1:** An illustration for constructing a solution

The proposed algorithm for tasks scheduling (BTS_ACO) follows the standard ACO algorithm that is used for static combinatorial optimization problems but with new features. The algorithm performs as follow: at each cycle, every ant constructs a solution and then the pheromone trials for each ant are updated with a value which depends on the solution constructed by the ants. The ant that constructs the best solution will have the higher amount of pheromone update. The algorithm stops iterating when the maximum number of cycles is reached. The Pseudo-code of the complete algorithm (BTS_ACO) is presented in Figure 2.

```
Algorithm: BTS_ACO

Initializing data
For each ant k in 1 … num_ant do

    produce candidate solution randomly
    Update pheromone
    Save best solution
    Update pheromone for best solution

Repeat

    For each ant k in 1 … num_ant do
```
{ // begin for ant
    Construct solution as the following
    - Select the first task \( t \) randomly and assign it to a processor
      \( T = T \cup \{ t \} \)
      Repeat
      { Select tasks depending on the property value \( p \) as given in equation 2
      }
      While \( T \neq \emptyset \)
      Update pheromone
      Save best solution
      Update pheromone for best solution
    } //end for ant
}

Update pheromone trial as follows:
if (\( M_s < M_g \)) then
  \( B_{star} = S_{save} \)
  \( M_g = M_s \)
For every edge between two tasks do
  \( \tau(t(t_1,t_2)) = \tau(t(t_1,t_2)) + q \)
For every edge between two tasks do
  \( \tau(t(t_1,t_2)) = \rho \times \tau(t(t_1,t_2)) \)
} Until (terminated condition is reached)

Figure 2: The steps of the BTS_ACO algorithm.

**Pheromone Trials and Heuristic Information**

In this step the pheromone matrix is initialized to equal amount of pheromone. In the next step, every ant constructs its own solution; after that the pheromone trial for each edge in the solution is updated with a value which depends on the solution constructed by the ants. Typically, the edges of the best solution will have the higher amount of pheromone update.

**Constructing a Solution**

In BTS_ACO algorithm each ant starts from a randomly selected task, and then it selects the next task from those unselected tasks depending on the property value \( p \) as given in the next formula [23].

\[
P_{a,c}^k(t) = \frac{t_{a,c}^\alpha(t) \cdot h_{a,c}^\beta(t)}{\sum_{a \in u(t)} t_{a,c}^\alpha(t) \cdot h_{a,c}^\beta(t)}\quad \text{Equation 2}
\]

Where \( k \) denotes the ant number,

\( P_{a,c}^k \) is the probability with which ant \( k \) chooses to select task \( a \) with set of tasks in processor \( c \),

\( t \) denotes the iteration numbers,

\( u \) denotes the set of task that are not visited yet,
\( I_{a,c} \) is the sum of pheromone value between task a and set of task in processor c,
\( h_{a,c} \) is the heuristic function which was chosen to be the inverse of the maximum difference of execution time between set of processor if we add task a to processor c at iteration t, 
\( \alpha \) and \( \beta \) are parameters that control the pheromone trials and the heuristic information.
The construction process is stopped when the maximum number of cycles is achieved.

**Pheromone Update**

After each ant has constructed a solution, pheromone trails are updated on each edge. The ant that constructs the best solution (bs) will have the higher amount of pheromone update. In BTS_ACO, pheromone is updated according to the following formula:

\[
I_s(t+1) = \rho I_s(t) + \frac{q}{\rho}
\]

Equation 3

Where \( I_s \) is the amount of pheromone between tasks in schedule s at time t,
\( I_s(t+1) \) is the amount of pheromone between tasks in schedule s at next iteration,
\( q, \rho \) is a given constant values.

While for other schedule, the pheromone trails are updated using the following formula:

\[
I_j(t+1) = \rho I_j(t)
\]

Equation 4

**5. EXPERIMENTAL RESULTS**

In this section, we used the simulation results to show the performance of the proposed BTS_ACO algorithm in a task scheduling system. The simulation programs are performed on Intel Core i3 2.2 GHz machine with 4 GB RAM. Table1 below shows the computational workloads used in the simulation.

<table>
<thead>
<tr>
<th>Parameters</th>
<th>Values</th>
</tr>
</thead>
<tbody>
<tr>
<td>Number of tasks</td>
<td>8-32 task</td>
</tr>
<tr>
<td>Execution time of tasks</td>
<td>10- 800 (seconds)</td>
</tr>
<tr>
<td>Number of CPUs</td>
<td>4 homogeneous CPUs</td>
</tr>
</tbody>
</table>

The ACO algorithm parameters values are shown in Table 2.

<table>
<thead>
<tr>
<th>A</th>
<th>B</th>
<th>Lamda</th>
<th>Ants</th>
<th>q0</th>
</tr>
</thead>
<tbody>
<tr>
<td>0.5</td>
<td>1</td>
<td>0.9</td>
<td>4</td>
<td>0.1</td>
</tr>
</tbody>
</table>

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To show the performance of BTS_ACO for RLoT and SLoT, the number of tasks was varied from 8 to 16 to 32 and measured the load balance, time of schedule creation and makespan. Information about the tasks chosen is shown in table 3.

<table>
<thead>
<tr>
<th>Number of tasks</th>
<th>Total Execution Time (sec)</th>
<th>Average Execution time (sec)</th>
</tr>
</thead>
<tbody>
<tr>
<td>8 task</td>
<td>2165</td>
<td>541</td>
</tr>
<tr>
<td>16 task</td>
<td>4565</td>
<td>1141</td>
</tr>
<tr>
<td>32 task</td>
<td>8144</td>
<td>2036</td>
</tr>
</tbody>
</table>

Figure 3 shows the comparison of RLoT and SLoT with respect to load balancing. The numbers shown for load balancing is actually the difference between the maximum load and minimum load among all CPUs in the system for a certain schedule. As this number decreases this indicates that the system is capable of distributing the tasks fairly to the CPUs. Load Balance of zero means that all the CPUs have the same amount of work to do. SLoT is capable of balancing the load more effectively to CPUs as shown in the figure.

Figure 4 shows the time each model needs to create the best schedule. As shown in the figure SLoT outperforms RLoT in this point.
Figure 5 shows the makespan time of tasks for each model. As mentioned above the makespan is the time needed to complete all the tasks and take results. Again the performance of SLoT is better than that of RLoT. The figure also shows that as the number of tasks increases, the difference between makespan and the average Execution time shown in Table 3 becomes smaller. The reason for this is that with higher number of tasks, there will be more tasks and alternatives to schedule.

![Figure 5. Makespan time of SLoT and RLoT](image)

6. CONCLUSION AND FUTURE WORK

In this paper we applied the ant colony optimization to the task allocation problem. The tasks to be scheduled were presented in a random (RLoT) and sorted (SLoT) form. The performance of BTS-ACO using SLoT outperforms the performance of BTS-ACO using RLoT in terms of load balancing, schedule create time and makespan time. The future work will examine the performance of BTS-ACO in a fault-tolerant system in addition to applying other different heuristic based algorithms for task allocation problem.

REFERENCES


