AN IMPROVED DECISION SUPPORT SYSTEM BASED ON THE BDM (BIT DECISION MAKING) METHOD FOR SUPPLIER SELECTION USING BOOLEAN ALGEBRA

Gabriel Almazán¹

¹IndustrialEngineering Educational Program, Superior School of Tepeji, Basic Sciences Institute, Autonomous University of Hidalgo, México

ABSTRACT

Based on the BDM (Bit Decision Making) method, the present work presents two contributions: first, the illustration of the use of the technique known as SOP (Sum Of Products) in order to systematize the process to obtain the correlation function for sub-system's mathematical modelling, and second, the provision of capacity to manage a greater than binary but a finite - discrete set of possible subjective qualifications of suppliers at any criterion.

KEYWORDS

Supplier Selection, Decision Support Systems, BDM (Bit Decision Making), Multi Criteria Decision Analysis, Boolean Algebra.

1. INTRODUCTION

The present work focuses on providing a contribution to the BDM(Bit Decision Making) method reported on [1]. In order to accomplish this, we give some basic conceptual and theoretical references that will provide a full operative mechanism to obtain the correlation function that relates the logic binary values assigned to suppliers by the decision maker(s) (inputs) with each sub-system output decision. As a consequence of this, an additional benefit will be the provision of capacity to qualify suppliers in more than just two ways ("yes" or "no"), but in a finite-discrete set of values.

In section 2 we give a brief exposition of BDM method and identify the opportunity areas in the initial proposal, where we visualize our contributions. In section 3 we present the conceptual and theoretical framework that will enable the BDM method to manage a discrete set of values for supplier qualifications. In section 4, we illustrate the application of the conceptual and theoretical background to the case presented at [1]. Finally, at section 5 we propose a variation on a specific sub-system to visualize implications and the benefit of our proposal.

2. THE BDM METHOD

2.1. A brief description

In BDM method, the decision will be reached considering every supplier's performance on subsystems of the form shown in Table 1.

Decision Criteria Pattern Number	First Criterion	Second Criterion	•••	Nth Criterion	Output
1	yes/no	yes/no	yes/no	yes/no	Yes/No
2	yes/no	yes/no	yes/no	yes/no	Yes/No
	yes/no	yes/no	yes/no	yes/no	Yes/No
Mth Pattern	yes/no	yes/no	yes/no	yes/no	Yes/No

Table 1. Truth Table structure for any sub-system.

The decision maker will configure the truth table by choosing the criteria combinations that will output a "Yes" or "No" result. Therefore, each sub-system acts as a filter for suppliers. If the output is "Yes", the supplier can continue to the next sub-system, otherwise it will be disqualified, and so on until reaching the last sub-system.

2.2. Opportunity Areas Identification

As can be seen in the reference paper [1], the way in which the logical function (that correlates inputs and output in each sub-system) is generated, is not specified. On the other hand, the original method is not able to manage a ranking scheme in supplier's performance qualifications at any criterion; for instance, the following degrees:excellent, good, average, poor.

3. CONCEPTUAL AND THEORETICAL REFERENCES 3.1. Number of possible patterns

According to combinatorics, the total number of patters for a truth table of N binary variables will be 2^{N} .

3.2. The SOP (Sum Of Products) Technique

To obtain a logical function that correlates binary inputs with a binary output, there are two options: in a Sum Of Products (SOP) or in Product Of Sums (POS) form. The Sum of Products (SOP) form will contain a list of terms in which all variables are ANDed (products), then ORed (summed) together. To convert a truth table to a SOP expression, only the rows whose output is "Yes" will produce a term. This AND term should produce a "Yes" with the values of variables in that row; hence, all the variables with value "no" should be logically complemented (inverted).

3.3. The minimal form

Boolean algebra axioms and theorems or Karnaugh maps (a graphical tool) could be used in order to find the minimal expression of the logical function that correlates inputs and the output. Basically, this tools help to identify which variables within a term -considerated jointly with other terms, become irrelevant.

3.4. Binary Coding

A set of things (characters, symbols, values, etc.) can be represented with a group of bits. Being x the number of objects, the number of bits required (n) can be calculated with:

$$n = \frac{\log x}{\log 2}$$

4. ILLUSTRATIVE APPLICATION OF THEORETICAL BACKGROUND. 4.1. Methodology to obtain sub-system's correlation function 4.1.1. From truth table to correlation function

Let us take the "Business Strengths evaluation phase" presented at [1] and obtain its mathematical model. First, we'll need one bit to encode the "yes" and "no" supplier's qualifications; let us assign "1" and "0", respectively. The resulting truth table is shown in Table 2.Additionally, let us apply the SOP technique. In doing so, we'll obtain the product terms shown in the last column. (Note: the symbol "l" indicates binary complement or "NOT" monary logic operator).

Decision	X3	X4	X5	X6	X7	Output	Product Term
Criteria						Y2	
Pattern Number							
1	0	0	0	0	0	0	
	0	Х	Х	Х	Х	0	
16	0	1	1	1	1	0	
17	1	0	0	0	0	0	
18	1	0	0	0	1	0	
19	1	0	0	1	0	0	
20	1	0	0	1	1	1	X3.X4I.X5I.X6.X7
21	1	0	1	0	0	Х	
22	1	0	1	0	1	Х	
23	1	0	1	1	0	Х	
24	1	0	1	1	1	X (1)	X3.X4I.X5.X6.X7
25	1	1	0	0	0	0	
26	1	1	0	0	1	1	X3.X4.X5 .X6 .X7
27	1	1	0	1	0	1	X3.X4.X5I.X6.X7I
28	1	1	0	1	1	1	X3.X4.X5I.X6.X7
29	1	1	1	0	0	0	
30	1	1	1	0	1	1	X3.X4.X5.X6l.X7
31	1	1	1	1	0	1	X3.X4.X5.X6.X7I
$32 = (2^5)$	1	1	1	1	1	1	X3.X4.X5.X6.X7

Table 2. Truth Table for the Business Strengths phase.

Thus, considering all rows with "1" as output, the initial sub-system mathematical model would be:

The symbol "X" on output means that the value could be either "0" or "1", as is impossible that a supplier has 3 last financial years of business positive turnover (profit), while no 1 or 2 years. We'll decide about this during the minimization process, as will be shown forward.

4.1.2. Finding the minimum expression with Boolean Algebra Axioms

In order to find the minimal expression of Y2, the following axioms of Boolean algebra can be applied, being X, Y and Z, Boolean variables.

i.	$\mathbf{X} \cdot \mathbf{Y} = \mathbf{Y} \cdot \mathbf{X}$	(commutativity)
ii.	$\mathbf{1.X} = \mathbf{X} \tag{ic}$	lentity, the neutral on the product)
iii.	$\mathbf{X} + \mathbf{X} = \mathbf{X}$	(idempotency)
iv.	$ \mathbf{X} + \mathbf{X} = 1$	(complementarity)
v.	$\mathbf{X} + (\mathbf{Y} + \mathbf{Z}) = (\mathbf{X} + \mathbf{Y}) + \mathbf{Z})$	(associativity)
vi.	$\mathbf{X}.(\mathbf{Y} + \mathbf{Z}) = (\mathbf{X}.\mathbf{Y}) + (\mathbf{X}.\mathbf{Z})$	(distributivity)

Thus, Y2can be rewritten as:

Y2 =(X3.X4.X5|.X6|.X7 + X3.X4.X5|.X6.X7 +X3.X4.X5.X6|.X7 +X3.X4.X5.X6.X7) +

(X3.X4.X5|.X6.X7| + X3.X4.X5.X6.X7| + X3.X4.X5|.X6.X7 + X3.X4.X5.X6.X7) +

(X3.X4I.X5I.X6.X7 + X3.X4.X5I.X6.X7 + X3.X4I.X5.X6.X7+X3.X4.X5.X6.X7)

Term in red colour corresponds to "X" term. Looking at Table 2, the product terms considered were:(26,28,30,32) + (27,31,28,32) + (20,28,24,32). The term 28 and 32 can be reused because of axiom *iii*.

Applying axioms *i*, *vi*, *iv* and *ii*:

Y2 = (X3.X4.X5I.X7.(X6I+X6) + X3.X4.X5.X7.(X6I+X6)) +

(X3.X4.X6.X7|.(X5| + X5) + X3.X4.X6.X7.(X5|+X5)) +

(X3. X5I.X6.X7.(X4I. + X4) + X3.X5.X6.X7.(X4I.+X4))

= (X3.X4.X5|.X7+X3.X4.X5.X7) +

(X3.X4.X6.X7|+X3.X4.X6.X7) +

(X3. X5I.X6.X7+ X3.X5.X6.X7)

Then, Y2 can be finally minimized:

Y2=X3.X4.X7 + X3.X4.X6 + X3.X6.X7

If, as in [1], X3 should be "1", Y2 can even reach the following form:

Y2 = X4.X7 + X4.X6 + X6.X7

4.1.3. Finding the minimum expression with Karnaugh maps

If we apply, as another alternative, Karnaugh maps, the resulting one will look as shown in Figure 1:

X3X4X5	000	001	011	010	110	111	101	100
X6X7								
00							Х	
01					1		Х	
11							1	1
10					1		Х	

Figure 1. Karnaugh Map the Business Strengths phase.

Groups of a 2^n number of "1's" should be identified, each of them generating a term in the output function; the larger the group the minimum of variables in the term. In this case, the three 4 ones

size possible groups are: 1) cells in orange, generating the term:X3.X6.X7, which contains the variables who don't change, disappearing X3,X4,X5 who do change; 2) cells in horizontal lines, generating the term: X3.X4.X7; and 3) cells in vertical lines, generating the term: X3.X4.X6.

Hence, Y2 = X3.X4.X7 + X3.X4.X6 + X3.X6.X7, the same obtained with Boolean algebra axioms.

In Karnaugh maps, any combination of the values of all input variables placed on any physical adjacent cell will have only a bit change between them. For example, first row-first column (000000) is adjacent with first row-second column (00100). Moreover, first row-first-column (00000), even not physically adjacent, will be logically with first row-eighth column (10000).

As can be seen in the example, "1's" can be reused, due to the fact that with Karnaugh maps we are implicitly and graphically applying the Boolean algebra axioms.

Therefore, the three groups in Figure 1 are of adjacent one's, eliminating as:

$$n = \frac{\log x}{\log 2}$$

variables associated with each group. In this case, all groups were 8 bits long, and so, two variables were eliminated from each term.

To demonstrate that this function performs identically with the version on [1], we create the Excel sheet shown in Figure 2.

C		7 - (*		Ŧ					Ijo	urnal - Mic	rosoft Excel				-		×
0	Inici	o Ir	nserta	ar	Dis	eño	de pá	igina Fói	rmulas	Dato	s Revisar	Vista				🥝 –	⊂ ×
	× 1	Cal	ibri		- 11	L -		= = =		General	• A	¦a•= Ins	ertar -	Σ	an.		
		N	K	s	- A	A			a	\$ - %	000	🔐 Elin	ninar -		uru		
F	Pegar 🦪	EFF.	-	2 -	A			= = »·-		* 0 00 00 > 0	Estilos	For	mato -	✓ Ordena ✓ y filtrar	r Buscary	V	
Port	apapeles			uente	_		3	Alineación) G	Número	5		das		dificar		
FOI		201		-								<u></u>			umcar		
110 $f_{\text{c}} = O(Y(C10,Y(D10,G10)),O(Y(C10,Y(D10,F10)),Y(C10,Y(F10,G10))))$											*						
-	A	В	С	D	E	F	G	1	J	к	L	м	N	0	P	Q	-
2				Selec	tion C	riteri	a										
		Pattern															
3		No.	X3	x4	x5	x6	x7	Output (Y2)		English	Spanish						_
4		1	0	0	0	0	0	FALSO		AND	Y						_
5			0	×	×	x	×			OR	0						
6		16	0	1	1	1	1	FALSO		FALSE	FALSO						
7		17	1	0	0	0	0	FALSO		TRUE	VERDADERO						1
8		18	1	0	0	0	1	FALSO									
9		19	1	0	0	1	0	FALSO									
10		20	1	0	0	1	1	VERDADERO									
11		21	1	0	1	0	0	FALSO									
12		22	1	0	1	0	1	FALSO									
13		23	1	0	1	1	0	FALSO									
14		24	1	0	1	1	1	VERDADERO									
15		25	1	1	0	0	0	FALSO									
16		26	1	1	0	0	1	VERDADERO									
17		27	1	1	0	1	0	VERDADERO									
18		28	1	1	0	1	1	VERDADERO									
19		29	1	1	1	0	0	FALSO									
20		30	1	1	1	0	1	VERDADERO									
21		31	1	1	1	1	0	VERDADERO									
22		32	1	1	1	1	1	VERDADERO									-
14 4	→ → H	oja1	Hoja	2	Hoj	2	-	/		1	1	4	-	III	1		
List			noja	02 /	noj		Cal.							75%	0		•
-			1	_	-	11	1				-		and the second sec		0		
6	>							🦻 🗹		<u>ا ا</u>			ES	- 🛱 🕩	aill 🍪	06:38 27/03/	

Figure 2. Karnaugh Map the Business Strengths phase.

5. RESULTS

5.1. More than "yes" or "no" criteria qualification

Let us take now the case of "Financial Quotation evaluation phase" in [1] to illustrate how this capacity is provided. Let's allow the Development (X9) criteria to be evaluated with four

different degrees: excellent, good, average and poor. We'll code these with "11","10","01" and "00" 2-bit words, respectively. Besides, let's consider the policy to approve the suppliers qualified as "excellent" at "Development" (X9) criterion or those with at least an "average" note in combination with any other of the remaining criteria, X8 and X10. Thus, the resulting truth table will be as shown in Table 3.

Decision Criteria	X8	X	(9	X10	Output
Pattern Number		X9a	X9b		Y4'
1	0	0	0	0	0
2	0	0	0	1	0
3	0	0	1	0	0
4	0	0	1	1	1
5	0	1	0	0	0
6	0	1	0	1	1
7	0	1	1	0	1
8	0	1	1	1	1
9	1	0	0	0	0
10	1	0	0	1	0
11	1	0	1	0	1
12	1	0	1	1	1
13	1	1	0	0	1
14	1	1	0	1	1
15	1	1	1	0	1
$16 = (2^4)$	1	1	1	1	1

Table 3. Truth Table for Technical phase.

The corresponding Karnaugh map is shown in Figure 3.

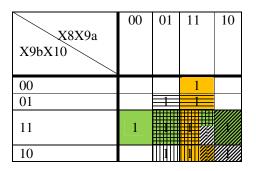


Figure 3. Karnaugh Map the Technical phase.

There are five groups of 4 one's, resulting in the following mathematical model:

Y4' = X8.X9a + X9a.X10 + X9b.X10+ X9a.X9b + X8.X9b

We can rewrite this on the following form:

Y4' = X8.(X9a + X9b) + X10.(X9a + X9b) + X9a.X9b

That will be easier to code as an Excel formula.

This correlation function can be introduced to the Excel spreadsheet and incorporated to the whole automated decision support system for getting the decision-result for this entity, at this phase.

6. CONCLUSIONS

With our proposal, the BDM method has been provided with the capacity to qualify suppliers in a wider way, with the provision of the mechanism to operate.

Future works can revise the Quine-Mc Cluskey numeric method to obtain sub-systems mathematical model or other methods that could be found in the literature or recently developed. Also, good opportunities are in the application of this framework at specific scenarios.

REFERENCES

- N. Jigeesh, (2012) "A New Decision Support System for Supplier Selection using Boolean Algebra", International Journal of Managing Public Sector Information and Communication Technologies, Vol. 5, No. 3, pp. 11-24.
- [2] P. Scherz, (2000) "Practical electronics for inventors", New York: McGraw-Hill.
- [3] R. Arnau,(2015) "The application of Boolean algebra to industrial engineering decision problems", Master in Science in Industrial Engineering, Texas Technological College.

Authors

Gabriel Almazán, M. in Sc. (Telecommunications Engineering), Master (Educational Technology), working as a Full Time Lecturer and Researcher at Autonomous University of Hidalgo, México. Some of the topics he teaches are Industrial and Digital Electronics. His research interests include Business Intelligence, Sustainability, Industrial Symbiosis, Educational Technology, revitalization of native Mexican languages andself, cooperative and collaborative learning.

