

# EVALUATION OF INFORMATION RETRIEVAL SYSTEMS

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## **ABSTRACT**

*One of the challenges of modern information retrieval is to adequately evaluate Information Retrieval System (IRS) in order to estimate future performance in a specified application domain. Since there are many algorithms in literature the decision to select one for usage depends mostly on the evaluation of the systems' performance in the domain. This paper presents how visual and scalar evaluation methods complement one another to adequately evaluate information retrieval systems. The visual evaluation methods are capable of indicating whether one IRS performs better than another IRS fully or partially. An overall performance of IRS is revealed using scalar evaluation methods. The use of both types of evaluation methods will give a clear picture of the performance of the IRSs. The Receiver Operator Characteristic (ROC) curve and Precision-Recall (P-R) curve were used to illustrate the visual evaluation methods. Scalar methods notably precision, recall, Area Under Curve (AUC) and F measure were used.*

## **KEYWORDS**

*ROC curve, Precision, Recall, Area Under Curve, Information Retrieval System*

## **1. INTRODUCTION**

Evaluation is very crucial and tedious task in information retrieval system. There are many retrieval models, algorithms and systems in literature so in order to proclaim the best among many, choose one to use and improve there is need to evaluate them. One way to evaluate is to measure the effectiveness of the systems. The difficult of measuring effectiveness is that it is associated with the relevancy of the retrieved items. This makes relevance the foundation on which information retrieval evaluation stands. Thus it is important to understand relevance. In order to support laboratory experimentation in the early studies, relevance was considered to be topical relevance, a subject relationship between item and query. According to [1] relevance is seen as a relationship between any one of a document, surrogate, item, or information and a problem, information need, request, or query. Relevancy from the human perspective is subjective (depends upon a specific user's judgement), situational (relates to user's current needs), cognitive (depends on human perception) and dynamic (changes over time). With the problems associated with relevance, it is very difficult to implement user-oriented evaluation of the system and it requires many resources. This problem of relevance has been researched in textual and non-textual environments [1, 2]. As a result, information retrieval evaluation experiments attempt to evaluate the system only [3]. An objective expert is then used to judge the

relevance of a document/item to one information need. There are many algorithms to evaluate the retrieval systems and can be classified into those that are used to evaluate ranked or unranked retrieval results [4]. They can also be regrouped into visual (graphical techniques) and scalar (non-visual techniques) [5]. The overview of the classification of the techniques is shown in Figure 1.

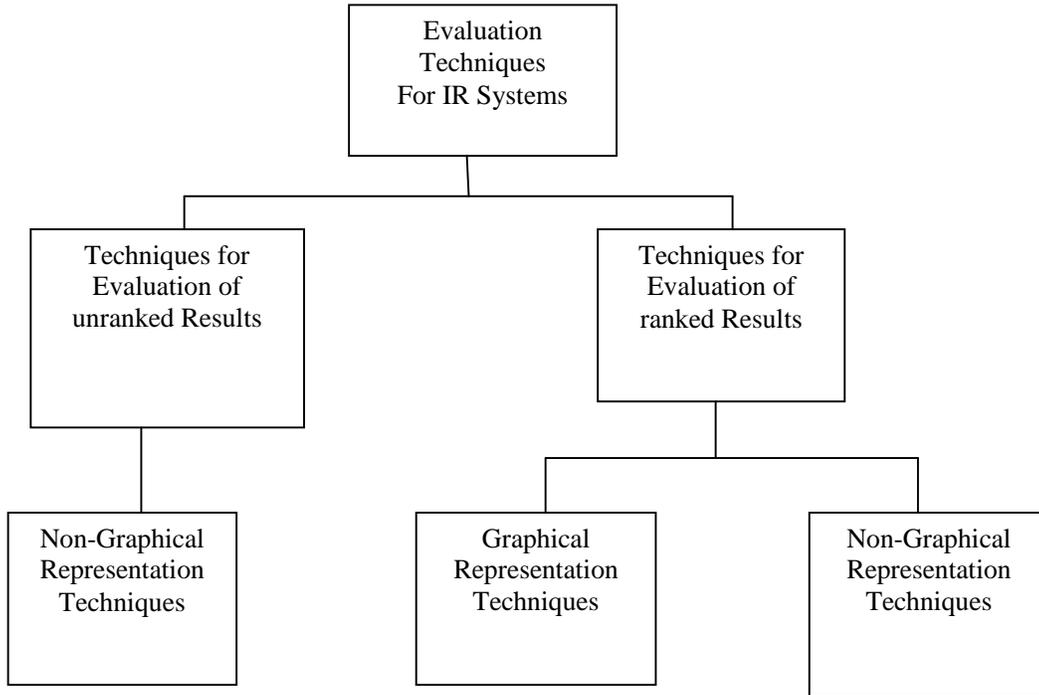


Figure 1: Hierarch of classification of evaluation techniques for IR systems

In this brief review of the evaluation techniques for information retrieval system, the following techniques will be reviewed using the classification in Figure 1: Precision, Recall, F-measure, Precision-Recall curve, Mean Average Precision, Receiver Operating Characteristics (ROC) curve and Area Under ROC Curve (AUC). The merits and demerits of these techniques will be discussed then investigate criteria to choose the appropriate algorithm(s) to use in different situations. Finally open issues will also be discussed and then conclusion.

## 2. TECHNIQUES FOR EVALUATION OF UNRANKED RETRIEVAL RESULTS

The most frequently and important basic measures for information retrieval effectiveness are precision and recall [3, 4]. Precision can be defined as the fraction of retrieved items that are relevant to all retrieved items or the probability given that an item is retrieved it will be relevant and recall as the fraction of relevant items that are retrieved to relevant items in the database or the probability given that an item is relevant it will be retrieved [4]. These notions can be made clear by examining the following set diagram (Figure 2). Figure 2 indicates the most important components of these measurements and formulas can be derived from it.

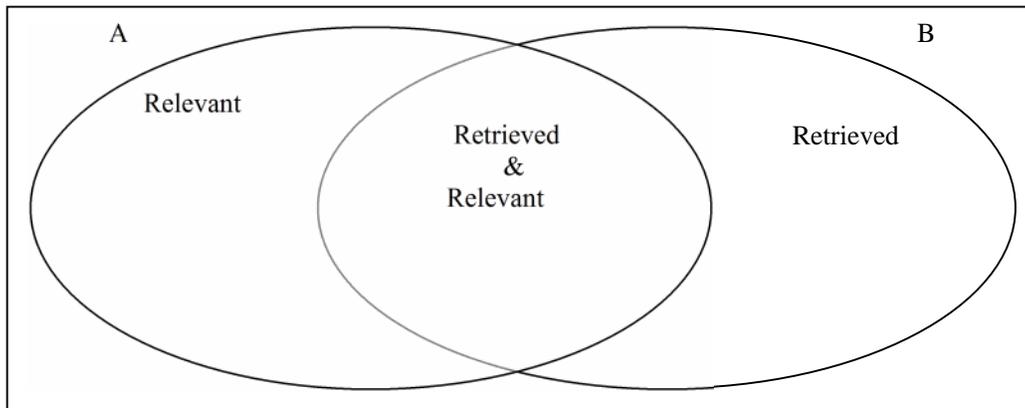


Figure 2: Set Diagram showing elements of Precision and Recall

The formulas for Precision (P) and recall (R) using set notation are in equation 1 and 2:

$$P = \frac{n(A \cap B)}{n(B)} \quad (1)$$

$$R = \frac{n(A \cap B)}{n(A)} \quad (2)$$

To the user the scalar value of recall indicates the ability of the system to find relevant items as per query from the collection of different items and precision ability to output top ranked relevant items as per query. In general the user is interested in the relevant retrieved items thus the measures of precision and recall concentrate the evaluation on the relevant output of the system. The lower the values indicates bad performance of the system and the higher the values the more the user is encouraged to use the system due to the anticipation of getting more of the relevant search items. These evaluation measures are inter-dependent measures in that as the number of retrieved items increases the precision usually decreases while recall increases.

From these measures there are other measures that are derived from them. F-measure is one known measure derived from precision and recall measures. This is scalar quantity that trade off precision versus recall which is the weighted harmonic mean of precision and recall. The formula is given in the equation below [6, 7]:

$$F = \frac{1}{\alpha * \frac{1}{P} + (1 - \alpha) * \frac{1}{R}} \quad (3)$$

where  $\alpha \in [0, 1]$ . The default balanced F measure equally weights precision and recall, which means making  $\alpha = \frac{1}{2}$ . The weights can be varied as required.

It is important to note that precision, recall and F measure are set oriented measures thus cannot adequately be used in ranked results systems [3].

### 3. TECHNIQUES FOR EVALUATION OF RANKED RETRIEVAL RESULTS

This section describes techniques for evaluation of ranked information retrieval results. Among these techniques are Precision-Recall curve (P-R-curve), ROC curve, R-precision, Mean Average Precision (MAP), ROC Area Under Curve and Precision at k just to mention a few.

Most current systems present ranked results thus to be able to use the precision and recall measures there is need to pair them at each given position. Considering the first  $k$  retrieved items, the precision and the recall values can be calculated as long as the total relevant items are known in the database. The following example illustrates the construction of the precision-recall curve.

Table 1: Showing the calculation of precision-recall coordinates

Calculating Precision-Recall Points											
Query Item=I56	Known #relevant items in database=5										
$R_p$	1	2	3	4	5	6	7	8	9	10	11
ItemID	I2	I33	I12	I8	I67	I99	I5	I1	I23	I3	I9
Relevance	Yes	No	Yes	Yes	Yes	No	No	No	No	No	Yes
Recall Value ( $r'$ )	1/5=0,2	1/5=0,2	2/5=0,4	3/5=0,6	4/5=0,8	4/5=0,8	4/5=0,8	4/5=0,8	4/5=0,8	4/5=0,8	5/5=1,0
Precision Value	1/1=1,0	1/2=0,5	2/3=0,67	3/4=0,75	4/5=0,8	4/6=0,67	4/7=0,57	4/8=0,5	4/9=0,44	4/10=0,4	5/11=0,45

From table 1  $R_p$  is the ranked position of an item retrieved and ItemID is the item identification. It can also be observed that when the item on  $R_{p+1}$  is not relevant the recall remains the same and precision decreases as shown in Table 1 when  $R_{p+1}=2$ , recall remained 0,2 as it was in  $R_p=1$ , precision decreased from 1,0 to 0,5. In case where the item in  $R_{p+1}$  is relevant the recall increases and the precision increases or remains the same. The P-R graph is the plotted from the precision-recall values in Table 1. The graph can be seen in Figure 2 with points marked using stars that have distinct saw-tooth shape. In order to smoothen the graph the interpolated precision is used and the interpolated precision  $\hat{P}$  at certain recall level  $r$  is defined as the maximum precision found for any recall level  $r'$  as in equation 4.

$$\hat{P}(r) = \max_{r' \leq r} p(r') \tag{4}$$

Interpolate a precision value for each standard recall level in Table 1 and the following Table 2 of 11-point interpolated average precision is obtained.

Table 2: 11-Point Interpolated Average Precision

$r'$	0,2	0,2	0,4	0,6	0,8	0,8	0,8	0,8	0,8	0,8	1,0
R	0,0	0,1	0,2	0,3	0,4	0,5	0,6	0,7	0,8	0,9	1,0
$\hat{p}(r)$	1,0	1,0	1,0	0,67	0,67	0,75	0,75	0,80	0,8	0,45	0,45

So the graph in first curve marked with \* in Figure 2 is transformed to the second curve whose points are marked with "X".

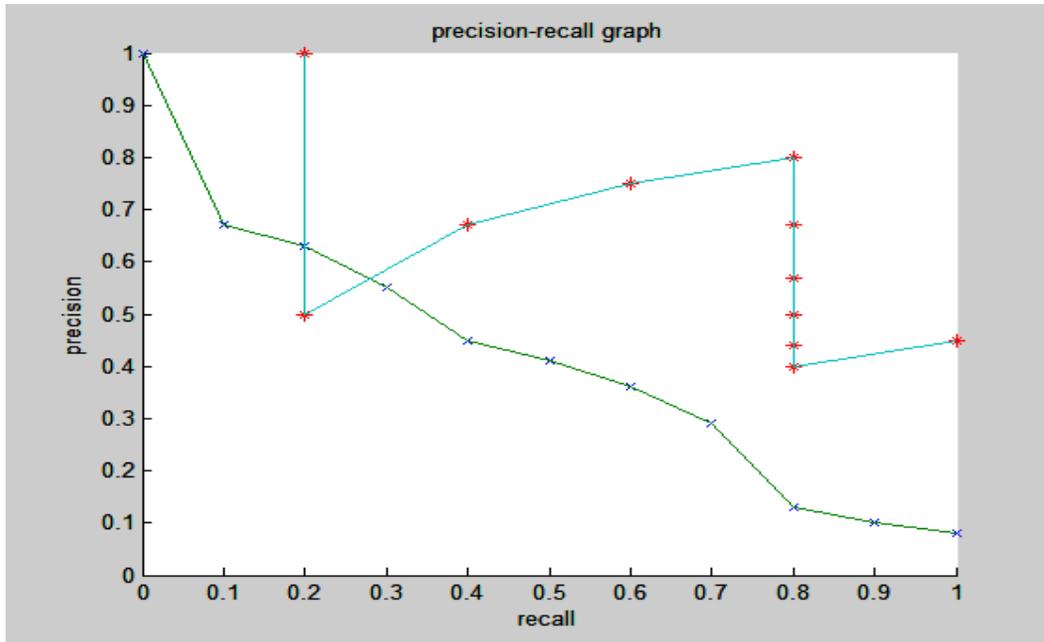


Figure 3: Graphs for values in Table 1 and Table 2

For more variations of Precision-Recall curves consult [4, 6].

Looking at non graphical evaluation techniques related to precision and/or recall, there is MAP which has gained popularity among the Text Retrieval Conference (TREC) members [4]. MAP is one of the various ways of combining precision and recall into a single scalar value measure which is defined as an average of the average precision value for a set of queries. Average precision is calculated by averaging the precision for every position in the ranking at which a relevant item is retrieved. Relevant items not retrieved by cut-off depth are assigned a precision of zero. The scalar value obtained is approximately equal to the area under the precision-recall curve. MAP expresses the quality of the system in one number. The formula that is used to calculate the MAP is given in equation 5.

$$MAP = \frac{1}{n(\text{Re})} \sum_{k=1}^k \text{Re}_k \frac{\sum_{i=1}^k \text{Re}_i}{k} \quad (5)$$

where  $n(\text{Re})$  is the number of relevant items,  $\text{Re}_k$  and  $\text{Re}_i$  take zero or one indicating not relevant or relevant at position  $k$  and  $i$  respectively.

There are other measures like Precision at  $k$  and R-precision that can be used. Precision at  $k$  shortened as  $P@k$  is the precision calculated at a cut-off point  $k$ . This measure does not measure recall. It is criticized in that relevance items for a query have a lot of influence on precision at  $k$  but is ignored. In order to alleviate this problem R-precision measure is introduced. In this

measure the number of relevant items is known and it becomes the cut-off point. The formula is given in equation 6:

$$R - Precision = \frac{1}{n(\text{Re})} \sum_k^{n(\text{Re})} \text{Re}_k \quad (6)$$

The R-precision measure is also called break-even point. R-precision refers to the best precision on the precision-recall curve.

Receiver Operating Characteristics curve is also used in information retrieval systems performance evaluation. In order to illustrate how ROC works it is important to understand the confusion matrix. A confusion matrix shows the differences between the true and predicted classes [8]. The confusion matrix is shown in Table 3.

Table 3: Confusion Matrix

	Actual Positive	Actual Negative	Total predicated
Predicated Positive	TP	FP	TP+FP=TPP
Predicated Negative	FN	TN	FN+TN=TPN
Total Actual	TP+FN=TAP	FP+TN=TAN	N

where TP is true positive (items correctly labelled as similar to query), FP false positive (items incorrectly labelled as similar to query item), FN false negative (items incorrectly labelled as not similar to query), TN true negative (items correctly labelled as not similar to query item), TPP total predicated positive, TPN total predicted negative, TAP total actual positive, TAN total actual negative and  $N = TAP + TAN = TPP + TPN$ . From the confusion matrix more meaningful measures can be derived from it to illustrate performance criteria as shown below [9, 10]:

$$TPR \text{ or } Sensitivity \text{ or } recall = \frac{TP}{TP + FN} = \frac{TP}{TAP} \quad (7)$$

$$FPR \text{ or } 1 - Specificity = \frac{FP}{FP + TN} = \frac{FP}{TAN} \quad (8)$$

TPR (True Positive Rate) measures the fraction of all relevant items in the database that have been correctly labelled similar to the query. FPR (False Positive Rate) measures the fraction of all irrelevant items in the database that have been incorrectly labelled similar to the query. These measures of performance are valid only for one particular operating point, an operating point normally being chosen to minimize the probability of error. The ROC curve is a plot of TPR versus FPR across different thresholds [11]. The TPR is plotted on the y-axis while FPR on the x-axis. Thus it offers a threshold-independent way of evaluating information retrieval performance. Usually a ROC curve always moves from the bottom left to the top right of the graph. Performance of a model represented as a point in an ROC curve. A good system produces results that generate a graph that climbs steeply on the left side as can be appreciated in Figure 4 (right hand side graph). The point (0, 0) indicates that everything to be negative class, (1, 1) indicates everything to be positive class and (0, 1) is the ideal situation. The diagonal line indicates a random guessing. Any point below the diagonal line predicts an opposite of the true class indicating a lower TPR and/or higher FPR [12, 13].

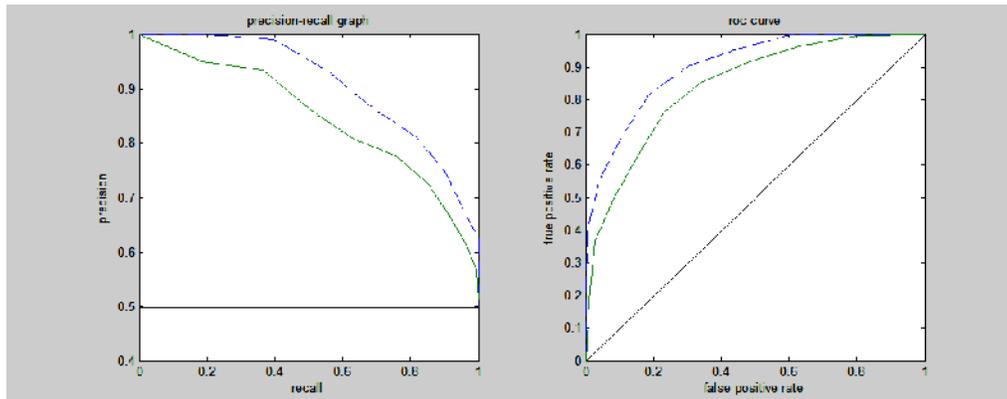


Figure 4: Graphs illustrating the appearance of P-R and ROC curves

The ROC curve also brings another form of measure of the performance of a system. This measure is ROC Area Under Curve (AUC) a simple scalar metric that defines how an algorithm performs over the whole space. The area can be calculated using the trapezoidal area created between each ROC curve points [13]. AUC value range is [0 1]. One indicates an ideal performance of a system, 0.5 a random guess performance of the system and a zero a system that never retrieves anything similar to the query [14]

#### 4. RELATIONSHIP BETWEEN ROC AND P-R RELATED MEASURES

The ROC and P-R curves are visual performance measures as seen in Figure 4. In [9] it is shown that a curve that dominates in ROC space also dominates in P-R space and vice versa. This is illustrated in Figure 4, the comparison of the two systems in P-R space and ROC space shows that system represented with dashed line performs better in both spaces. Again from these graphs it can be appreciated that the area under the curves in both spaces are approximately equal. In P-R space the area under the curve is called MAP and in ROC space ROC-AUC. The bigger the area the better the system performs.

#### 5. CONCLUSION

Performance evaluation is crucial at many stages in information retrieval system development. At the end of development process it is significant to show that the final retrieval system achieves an acceptable level of performance and that it represents a significant improvement over existing retrieval systems. To evaluate a retrieval system, there is need to estimate the future performance of the system. The information retrieval performance evaluation methods measures highlights different aspects of a model's classification performance and so selecting the most appropriate performance measure is clearly application dependent [10]. The scalar measures are attractive to use because they give a definitive answer to which retrieval system is better, this gives authors the authority to claim the superiority of their algorithm. The scalar measure gives an overall value of performance of the system and no any other information. The visual performance measure preserves all performance related information about a retrieval system. The visual performance measure is capable of showing if one system dominates the other system totally or partially.

The traditional binary evaluation methods play a dominate role in the history of information retrieval system evaluation. These methods include recall, precision, MAP, precision at k and R-

precision [7]. Precision-recall analysis has remained as the appropriate evaluation performance measures of choice in applications such as database image retrieval. Precision-Recall Curve (PRC) which plot precision vs recall across all thresholds represents a more natural way of looking at classification performance when it comes to search relevant items (information retrieval) in situations where the available data is heavily imbalanced in favour of the negative class [15]. The end-users relate to precision-recall curves as they indicate how many true positives are likely to be found in a typical search. Evaluation at single operating point is suitable in well defined environment where class priors and misclassification cost are known [1, 10].

ROC curve is helpful in assessing the performance of a system independently of any given threshold. The ROC curve which plot TPR vs FPR allows authors to quickly see if one method dominates another, and using convex hull to identify potentially optimal methods without committing to a specific performance measure. There is a scalar measure related to ROC curve which is ROC Area Under Curve (ROC-AUC) is also used to measure predictive system's performance.

There many other methods suggested in literature, they all fall within these two categories: Scalar and Visual measures. The few described above seem to be the mostly used in evaluation methods of information retrieval systems' performance.

Combining scalar and visual evaluation techniques of information retrieval systems gives a full picture and a definite answer about the performance of the system being evaluated. The following Table 4 gives the summary of the benefits of the techniques when used alone and when combined.

Table 4: Summary of benefits of using the evaluation techniques

<b>Evaluation Techniques</b>	<b>Result</b>	<b>Usage/Benefits</b>
Scalar Techniques (unranked results)	<ul style="list-style-type: none"> <li>• A single number</li> </ul>	<ul style="list-style-type: none"> <li>• Indicates a definite level of performance of the system</li> <li>• Can be used to numerically compare the performance of different systems</li> <li>• Gives a definite answer to the performance of the system</li> </ul>
Visual Techniques (ranked results)	<ul style="list-style-type: none"> <li>• Visual graph</li> </ul>	<ul style="list-style-type: none"> <li>• Indicates a visual performance of the system</li> <li>• Used to graphically compare the performance of systems</li> <li>• Gives a visual answer to the performance e.g. positions where the system performs best or badly</li> <li>• Anomalies can be seen and experiments can be repeated</li> </ul>
Scalar and Visual Techniques (ranked results)	<ul style="list-style-type: none"> <li>• Single number</li> <li>• Visual graph</li> </ul>	<ul style="list-style-type: none"> <li>• All the usages/benefits in scalar and visual techniques</li> </ul>

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